

# Seven Model Motivated Rules of Thumb or Equations

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# Notes on Nonresponse Presentation

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In the slides that follow much has been left unwritten because it was intended to be said. Those spoken words are not included here, although not to be too cryptic, I have added a few notes to hint at what I was trying to say.

# Notes on Nonresponse Presentation

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First, the (obviously vast) topic of nonresponse has been confined to unit nonresponse. No mention is made of item nonresponse, for example. Arguably many points carry over nonetheless.

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Second, the topic has been treated from an historical perspective, following the approach I have been taking in my History Corner series in *The American Statistician* (TAS). In this connection the November 2004 TAS issue may be of particular value, as it brings out some of my points in more detail.

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Third, the formulas provided are more LOGOS that prescriptions to be used in real life applications. They were part of the arguments that the original framers of these ideas used but are oversimplified. For example, most of these ideas would be imbedded in pre or post strata to give them more plausibility and content.

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Fourth, in some cases the formula has been associated in the slides with their author. But this has not always been done so each of authors of these formulas or rules has been given mention below.

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Fifth, the bias/variance tradeoff slide (No.1) was taken from the introductory chapters of the HHM (Hansen, Hurwitz and Madow) and Cochran sampling texts. Their result has been repeated here to introduce how our professional (over) emphasis on sampling was sold. Those texts carved out the sampling role from the much larger data collection issues - all too successfully it might be added.

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Sixth, the response (and implicitly nonresponse) bias factors formula (No.2), original with me, was an attempt to succinctly indicate how wrongly our practice continues to overemphasize sampling, even 50+ years later. We need to add significantly to our records the extensive paradata that is routinely assembled in our surveys and bring it forward to the client and to future survey developers.



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Seventh, the missingness mixture slides (Nos. 3 to 5) are my interpretation of Rubin's seminal work on missingness (Biometrika 1976), where the emphasis is on the ubiquity with which all forms of missing unit nonresponse existing simultaneously in nearly all practical settings. Our failure to act on this knowledge is a weakness in our practice.

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Eighth, the Hansen-Hurwitz subsampling idea for nonresponse is discussed next (No.6). Here the attempt is to illustrate how we could reinterpret their work using Rubin's idea of the multiple forms of missingness and, thereby, reduce the variance penalty if we have sufficient confidence in our missingness model. The interview mode change made as part of the original idea is sometimes lost and I regret that I did not say more about it last week.

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Ninth, the Sekar-Deming capture/recapture application to nonresponse (No. 7) concludes the talk, except for some discussion of implications. Since these ideas are familiar in their dual systems incarnation, there is less to say here than elsewhere.

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Tenth, the concluding discussion slides were just my take on our history. Many good suggestions were made for better terminology by those present. Several objected to Rubin's use of the phrase "Missing at Random," abbreviated as MAR. Why not say, instead, they argued, that if we have the right variables present (say in the frame), then we can condition on them and thus eliminate some of the bias.

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## 1. Bias versus Sampling Error

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1. Bias versus Sampling Error
2. Response Bias Factors
3. Mixtures of Missingness
4. Data Collection Missingness
5. Data Analysis Missingness
6. Subsamples for Nonresponse
7. "Bias" or Hard-Core Non-Response Rates

# 1. Bias versus Sampling Error

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$$\begin{aligned}\text{MSE}[f(Y)] &= \sqrt{\frac{\sigma^2}{n} + B^2} \\ &= \sqrt{\frac{\sigma^2}{n}(1 + R^2)}\end{aligned}$$

(e.g., as shown in the Hansen, Hurwitz and Madow text.)

## 2. Survey Bias Factors

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$$\int \int \int f(Y, M, R, C, D) dM dR dC = g(Y, D)$$

Implicitly, this formal integration symbolizes that final survey data files usually treat process fixes as complete. Leaving out the paradata concerning these flaws continues in a way the historical theme in slide No. 1.

# 3. Mixtures of Missingness

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In general

$$m = m_{\text{MCAR}} + m_{\text{MAR}} + m_{\text{NMAR}}$$

can become specialized at various survey stages



# 4. Data Collection Missingness

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Implicitly, given what is done

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## Some Alternatives

- Subsampling Solutions,  $m = m_{\text{NMAR}}$
- Previous Experience, See Example
- Adaptive Approach, Decide on Fly
- Enrich the Frame, Make More  $m = m_{\text{MAR}}$
- Use a Composite



# 5. Data Analysis Missingness

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$$m = m_{\text{MCAR}} + m_{\text{MAR}} + m_{\text{NMAR}}$$

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- Adaptively Balanced Adjustment
- Sensitivity Analysis
- Weight Trimming



# 6. Hansen-Hurwitz Formula

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$$\bar{y} = p_R \bar{y}_R + p_M \bar{y}_M$$

where

- $p_R$  = "responding" fraction of the original sample
- $p_M$  = remaining "non-responding" fraction of the original sample

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$$\hat{v}(\hat{y}) \approx p_R \frac{s_R^2}{n} + p_M \frac{s_M^2}{vn} + \frac{1}{n-1} [p_R(\bar{y}_R - \hat{y})^2 + p_M(\bar{y}_M - \hat{y})^2]$$

where  $v$  = sub-sampling rate and other terms, e.g.,  $s_R^2$ , are just the standard notation

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- If there are good covariates present
- Treat "Bulk" as  $m_R = m_{\text{MAR}} + m_{\text{MCAR}}$
- "Bulk" can sometimes be estimated?

# 7. Sekar-Deming "Bias" Rates

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- Include cases from first survey in second
- Unlike Hansen-Hurwitz, obtain both Respondents and Nonrespondents
- Create a  $2 \times 2$  Table where the cells are
  - $rr$  = responded both times
  - $rn$  = responded first time only
  - $nr$  = responded second time only
  - $nn$  = never responded



# 7. Capture/Recapture Table

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$$\left[ \begin{array}{c|c} rr & rn \\ \hline nr & nn \end{array} \right]$$

# 7. Potential Bias Rate

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$$dd = \frac{(rn)(nr)}{rr}$$

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$$dd = \frac{(rn)(nr)}{rr}$$

Then

$$bb = \frac{nn - dd}{m}$$

can be considered the potential bias rate

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- UI Nonprofit Nonresponse Rate = 27 %
- UI Nonprofit Potential Bias Rate = 11 %

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- NSAF Nonresponse Rate = 38 %
- NSAF Potential Bias Rate = 15 %
- NORC Sales Tax Nonresponse Rate = 79 %
- NORC Sales Tax Potential Bias Rate = 28 %



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- These Rules of Thumb obviously will not work everywhere but have been good starting points in many practical settings
- Some reallocation of resources in survey execution and adjustment seems worthy of consideration in such settings
- Estimating the missingness mixture fractions is key here. One way to do this has been proposed but more are needed

# Provide to End Users and Future Survey Designers

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- For example number of Calls, who was present, Language used, Length of interview, Data on case from Frame, etc
- Nonrespondent cases should also go forward as a final deliverable, with details like point of Breakoff, Frame characteristics, number and conditions around Attempts, etc



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- Keep safe identifiers of both respondents and nonrespondents for possible later use
- For bias reduction/analyses, as originally proposed, or for potential bias rate calculations, as described here
- Could greatly lower long-term costs, while improving quality and enhancing credibility

# Reanalysis Opportunities

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- Examine whether partnerships across organizations would have merit in measuring potential bias rates

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- Look at statements made to potential respondents, should a sample of them be purposely returned
- Examine confidentiality issues that might arise even if former response status of a case was to be disclosed
- Run cognitive tests of these ideas, for potential respondents and clients

THANK YOU...